UNIT-2 (Section-2)

RCS-603: COMPUTER GRAPHICS

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UNIT-2 Syllabus – Section 2 CHAPTER6Two-Dimensional Viewing Donal D. Hearn and M. Pauline Baker

Windowing and Clipping: Viewing pipeline, [Viewing transformations, 2-D Clipping algorithms- Line clipping algorithms such as Cohen Sutherland line clipping algorithm, Liang Barsky algorithm, Line clipping against non rectangular clip windows; Polygon clipping – Sutherland Hodgeman polygon clipping, Weiler and Atherton polygon clipping, Curve clipping, Text clipping

C H A P T E R 6 Two-Dimensional Viewing Donal D. Hearn and M. Pauline Baker

- 1. Windowing And Clipping: Viewing Pipeline
- 2. Viewing Transformations
- 3. 2-D Clipping Algorithms
 - 1. Line Clipping Algorithms Cohen Sutherland Line Clipping Algorithm
 - 2. Liang Barsky Algorithm
 - 3. Line Clipping Against Non Rectangular Clip Windows
- 4. Polygon Clipping
 - 1. Sutherland Hodgeman Polygon Clipping
 - 2. Weiler And Atherton Polygon Clipping
- 5. Curve Clipping
- 6. Text Clipping



Windowing and Clipping:

- It consider the formal mechanism for displaying views of a picture on an output device.
- For a two-dimensional picture, a view is selected by specifying a subarea of the total picture area.





Windowing and Clipping:

- A user can select a single area for display, or several areas could be selected for simultaneous display.
- Transformations from world to device coordinates involve translation, rotation, and scaling operations, as well as procedures for deleting those parts of the picture that are outside the limits of a selected display area.(clipping)





Windowing and Clipping:

 Transformations from world to device coordinates involve translation, rotation, and scaling operations, as well as procedures for deleting those parts of the picture that are outside the limits of a selected display area.(clipping)





- A world-coordinate area selected for display is called a window.
- Viewport
- An area on a display device to which a window is mapped is called a viewport.
- The window defines **what** is to be viewed; the viewport defines **where** it is to be displayed.







• Viewing Transformation.

• The mapping of a part of a worldcoordinate scene to device coordinates is referred to as a viewing transformation.





• Figure 6-1 illustrates the mapping of a picture section that falls within a rectangular window onto a designated & angular viewport.



Eigure 6-1

A viewing transformation using standard rectangles for the window and viewport.

- It consist a sequence of steps used to perform two dimensional viewing transformations
- The major steps are as follows



Figure 6-2

The two-dimensional viewing-transformation pipeline.

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- 1. We construct the scene in world coordinates
- 2. We then transform descriptions in world coordinates to viewing coordinates.
- 3. We then define viewport in normalized coordinates (in the range from 0 to 1)
- 4. At the final step, all parts of the picture that he outside the viewport are clipped, and the contents of the viewport are transformed to device coordinates.





Figure 6-3 Setting up a rotated world window in viewing coordinates and the corresponding normalized-coordinate viewport.





Normalized Coordinates

- Viewports are typically defined within the unit square (normalized coordinates).
- This provides a means for separating the viewing and other transformations from specific outputdevice requirements, so that the graphics package is largely device-independent.





Viewing Coordinate Reference Frame

(a) translate the viewing origin to the world origin,

(b) rotate to align the axes of the two systems.



Figure 6-4

A viewing-coordinate frame is moved into coincidence with the world frame in two steps: (a) translate the viewing origin to the world origin, then (b) rotate to align the axes of the two systems. Viewing Coordinate Reference Frame

• The composite two-dimensional transformation to convert world coordinates to viewing coordinate is

$$\mathbf{M}_{\mathsf{WC},\mathsf{VC}} = \mathbf{R} \cdot \mathbf{T} \tag{6-1}$$

 where T is the translation matrix that takes the viewing origin point P to the world origin, and R is the rotation matrix that aligns the axes of the two reference frames.







Figure 6-7

A point (xw, yw) in a world-coordinate clipping window is mapped to viewport coordinates (xv, yv), within a unit square, so that the relative positions of the two points in their respective rectangles are the same.



- We maintain the same relative placement in the viewport as in the window.
- If a coordinate position is at the center of the world window, for instance, it will be displayed at the center of the viewport.





• A point at position (*xw,yx*) in the window is mapped into position (*xv,yv*) in the associated viewport.



Figure 6-5

A point at position (*xw*, *yw*) in a designated window is mapped to viewport coordinates (*xv*, *yv*) so that relative positions in the two areas are the same.



• We maintain the same relative placement in the viewport as in the window.





Solving these expressions for the viewport position (xv, yv), we have

$$xv = xv_{\min} + (xw - xw_{\min})sx$$
$$yv = yv_{\min} + (yw - yw_{\min})sy$$

where the scaling factors are

$$sx = \frac{xv_{\max} - xv_{\min}}{xw_{\max} - xw_{\min}}$$
$$sy = \frac{yv_{\max} - yv_{\min}}{yw_{\max} - yw_{\min}}$$



2-D Clipping Algorithms



2-D Clipping Algorithms



- Clipping Any procedure that identifies those portions of a picture that are either inside or outside of a specified region of space is referred to as a clipping algorithm, or simply clipping.
- The region against which an object is to clipped is called a clip window.





Applications Of ClippIng

Applications of clipping include

- 1. Drawing and painting operations that allow parts of a picture to be selected for copying, moving, erasing, or duplicating.
- 2. Extracting part of a defined scene for viewing;
- 3. Identifying visible surfaces in three-dimensional vlews;
- 4. Antialiasing line *seg*ments or object boundaries;
- 5. Creating objects using solid-modeling procedures;
- 6. Displaying a multi window environment;



Types of clipping

- We consider algorithms for clipping the following primitive types
- 1. Point Clipping
- 2. Line Clipping (straight-line segments)
- 3. Area Clipping (polygons)
- 4. Curve Clipping
- 5. Text Clipping



Point Clipping

 we save a point P = (x, y) if it is inside the clipping window.





Point Clipping



Assuming that the clip window is a rectangle in standard position, we save a point P = (x, y) for display if the following inequalities are satisfied:

 $xw_{\min} \le x \le xw_{\max}$

 $yw_{\min} \leq y \leq yw_{\max}$

• where the edges of the clip window (xwmin, xwmin, ywmin, ywmin, ywmin) can be either the world-coordinate window boundaries or viewport boundaries. If any one of these four inequalities is not satisfied, the point is clipped (not saved for display).



Line Clipping Algorithms



Figure 6-7 Line clipping against a rectangular clip window.



Line Clipping Algorithms

- A line clipping procedure involves several parts.
- 1. First, we can test a given line segment to determine whether it lies completely inside the clipping window.
- 2. If it does not, we try to determine whether it **lies completely outside** the window.
- 3. Finally, we must perform intersection calculations with one or more clipping boundaries.





Cohen Sutherland Line Clipping Algorithm

Basic Idea:

- First, do easy test
 - *completely* inside or outside the box?
- If no, we will need to figure out how line intersects the box





Cohen Sutherland Line Clipping Algorithm

• Every line end point in a picture is assigned a four-digit binary code, called a region code, that identifies the location of the point relative to the boundaries of the clipping rectangle.

1

•	First bit set 1 : Point lies to left of window $\mathbf{x} < \mathbf{x}_{min}$	1001	0001	0101
•	Second bit set 1 : Point lies to \mathbf{right} of window $\mathbf{x} > \mathbf{x_{max}}$	1000	0000	0100
•	Third bit set 1 : Point lies below(bottom) window $\mathbf{y} < \mathbf{y_{min}}$	1000	0000	0100
•	fourth bit set 1 : Point lies above(ton) window y > y _{max}		Window	
LRBT (Left, Right, Bottom, Top).				
		1010	0010	0110

Cohen Sutherland Line Clipping Algorithm



Х



- Find color codes of the points
- P1(5,6) P2 (25,15) P2 (25,15)
- P4(15,60) P5 (15,15) P6 (25,40)



- First bit set 1 : Point lies to left of window $\| x < x_{min} \|$
- Second bit set $1 \ge$ Point lies to **right** of window $\mathbf{x} > \mathbf{x}_{max}$
- Third bit set 1 : Point lies below(bottom) window y < y_{min}
- fourth bit set 1 : Point lies above(ton) window y > y_{max}
 LRBT (Left, Right, Bottom, Top).

1001	0001	0101
1000	0000	0100
	Window	
1010	0010	0110












Cohen Sutherland Line Clipping Algorithm

Trivial Acceptance

- If the logical OR is **zero**, the line can be trivially accepted.
- For example, if the endpoint codes are 0000 and 0000, the logical OR is 0000 the line can be **trivially accepted.**
- If the endpoint codes are 0000 and 0110, the logical OR is 0110 and the line can not be trivally accepted.

1001	0001	0101
1000	0000	0100
	Window	
1010	0010	0110



Cohen Sutherland Line Clipping Algorithm

Trivial Rejection

- If the logical AND of the endpoint codes is **not zero**, the line **can be trivally rejected**.
- For example, if an endpoint had a code of 1001 while the other endpoint had a code of 1010, the logical AND would be 1000 which indicates the line segment lies outside of the window.
- On the other hand, if the endpoints had codes of 1001 and 0110, the logical AND would be 0000, and the line **could not be trivally rejected**.

1001	0001	0101
1000	0000	0100
	Window	
1010	0010	0110



Cohen-Sutherland Algorithm (2/2)

▶ $y = y_0 + slope \times (x - x_0)$ and $x = x_0 + (\frac{1}{slope}) \times (y - y_0)$

Algorithm:

ComputeOutCode(x0, y0, outcode0); ComputeOutCode(x1, y1, outcode1);

repeat

check for trivial reject or trivial accept pick the point that is outside the clip rectangle

if TOP then

x = x0 + (x1 - x0) * (ymax - y0) / (y1 - y0);y = ymax;

else if BOTTOM then

x = x0 + (x1 - x0) * (ymin - y0) / (y1 - y0);y = ymin; else if RIGHT then
 y = y0 + (y1 - y0) * (xmax - x0) / (x1 - x0);
 x = xmax;
else if LEFT then
 y = y0 + (y1 - y0) * (xmin - x0) / (x1 - x0);
 x = xmin;

if (x0, y0 is the outer point) then x0 = x; y0 = y; ComputeOutCode(x0, y0, outcode0)

else

x1 = x; y1 = y; ComputeOutCode(x1, y1, outcode1) until done



Cohen Sutherland Line Clipping Example

- Consider the line segment AD.
- Point A has an outcode of 0000 and point D has an outcode of 1001.
- The logical AND of these outcodes is zero; therefore, the line cannot be trivally rejected.
- Also, the logical OR of the outcodes is not zero; therefore, the line cannot be trivally accepted.
- The algorithm then chooses **D** as the outside point (its outcode contains 1's).
- By our testing order, we first use the top edge to clip **AD** at **B**. The algorithm then recomputes **B**'s outcode as **0000**.
- With the next iteration of the algorithm, **AB** is tested and is trivially accepted and displayed.



1001	0001	0101
1000	0000	0100
	Window	
1010	0010	0110



Cohen Sutherland Line Clipping Example

- Consider the line segment EI.
- Point E has an outcode of 0100, while point I's outcode is 1010.
- The results of the trivial tests show that the line can neither be trivally rejected or accepted.
- Point E is determined to be an outside point, so the algorithm clips the line against the bottom edge of the window.
- Now line EI has been clipped to be line FI.
- Line FI is tested and cannot be trivially accepted or rejected. Point F has an outcode of 0000, so the algorithm chooses point I as an outside point since its outcode is1010.



1001	0001	0101
1000	0000	0100
	Window	
1010	0010	0110

Cohen Sutherland Line Clipping Example

- Line FI is tested and cannot be trivially accepted or rejected.
- Point F has an outcode of 0000, so the algorithm chooses point I as an outside point since its outcode is1010.
- The line FI is clipped against the window's top edge, yielding a new line FH.
- Line FH cannot be trivally accepted or rejected. Since H's outcode is 0010, the next iteration of the algorthm clips against the window's right edge, yielding line FG.
- The next iteration of the algorithm tests FG, and it is trivially accepted and display.



1001	0001	0101
1000	0000	0100
	Window	
1010	0010	0110





Cohen Sutherland Line Clipping Algorithm

Y

- Numerical
- Find visible portion of the line between points
- P1(x0,y0) = (12,8)
- P2(x1,y1) = (15,15)





Curve Clipping

- Areas with curved boundaries can be clipped with methods similar to those discussed in the previous sections.
- Curve-clipping procedures will involve nonlinear equations, however, and this requires more processing than for objects with linear boundaries.





Curve Clipping : Complete accept or reject

- If the bounding rectangle for the object is **completely inside** the window, we save the object.
- If the rectangle is determined to be **completely outside** the window, we discard the object.
- But if the bounding rectangle test fails, we can look for other computation-saving approaches.





Curve Clipping : Complete accept or reject

- For a circle,
- we can use the coordinate extents of individual quadrants and then octants for preliminary testing (outside or inside) and then calculate curve-window intersections.





Text Clipping





Text Clipping

- Various techniques are used to provide text clipping in a computer graphics.
- It depends on the methods used to generate characters and the requirements of a particular application.
- There are three methods for text clipping which are listed below –
- 1. All or none string clipping
- 2. All or none character clipping
- 3. Text clipping



All or none string clipping

 In all or none string clipping method, either we keep the entire string or we reject entire string based on the clipping window.





All or none character clipping

In this method if the string is partially outside the window, then –

- 1. You reject only the portion of the string being outside
- 2. If the character is on the boundary of the clipping window, then we discard that entire character and keep the rest string.





Text clipping

- If it is partially outside the window, then
- 1. You reject only the portion of string being outside.
- 2. If the character is on the boundary of the clipping window, then we discard only that portion of character that is outside of the clipping window.





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Liang – Barsky clipping



- In computer graphics, the Liang–Barsky algorithm (named after You-Dong Liang and Brian A. Barsky) is a line clipping algorithm.
- The Liang–Barsky algorithm uses the parametric equation of a line and inequalities describing the range of the clipping window to determine the intersections between the line and the clipping window. With these intersections it knows which portion of the line should be drawn.
- This algorithm is significantly more efficient than Cohen–Sutherland.

Liang-Barsky Algorithm



- The Liang-Barsky algorithm is a line clipping algorithm.
- This algorithm is more efficient than Cohen–Sutherland line clipping algorithm and can be extended to 3-Dimensional clipping.
- This algorithm is considered to be the faster parametric line-clipping algorithm.

Liang-Barsky Algorithm



- The following concepts are used in this clipping:
- The parametric equation of the line.
- X = x0 + u(x1-x0)
- Y = y0 + u(y1-y0)
- The inequalities describing the range of the clipping window which is used to determine the intersections between the line and the clip window.
- xwmax <= x0 + u(x1-x0) <= xwmin
- ywmax <= y0 + u(y1-y0) <= ywmin

LIANG-BARSKY ALGORITHM
THIS ALGORITHM USES MARAMETRIC EQUATIONS OF LINE
to calculate and find out intersection points and
LIANG-BARSKY ALGORITHM.
To calculate and find outpace equations

$$More: 0 \ Uman = 0 \ Umax = 1 \ Ugy DEFAULT)$$

 $0 \ U_K = \frac{g_K}{f_K} \ (K' is constant)$
We consider values for 'K' and find multiple values of UK
(3) Umin $\leq 0 \ K \leq Umax$ (b) $0 \le U \ K \leq 1$
USE following inequatives to calculate g_K and p_K
 $P_0 = -\Delta X$ ($G_1 = Xmax - X_0$)
 $P_1 = \Delta Y$ ($G_2 = Y_0 - Ymin$
 $P_3 = \Delta Y$ ($G_3 = Y_0 - Ymin$
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 $P_3 = \Delta Y$ ($G_3 = Y_0 - Ymin$
 $P_3 = Y (G_3 = Y_0 - Ymin)$
 $P_3 = Y (G_3 = Ymin$

8) LET ABCD BE THE RELTANGULAR WINDOW WITH A (0,0)
B(10,0); C(10,10); D(0,10) USE UNKO BARSKY ACCORTINA
TO CLIP THE LINE POP, WITH POCS, 3); P((15, 9).

$$\Rightarrow$$
 STEP 1: PLOT THE POINTS.
 $y_{min} = 0$; $y_{max} = 10$
 $y_{min} = 0$; $y_{max} = 10$
 $g_{0}(-5,3)$
 $f_{0}(-5,3)$
 $f_{0}(-5,3$

CONSIDER VALUES OF UK IF IT SATISFIES Umin SUKS UMAX (i.r) OSUKSI. . WE CONSIDER UD = 0.27 AND U, = 0.75 STEP 4 : CALCULATE INTERSECTION POINTS STEP 5: Plot intersection () When U = 0.25 points and clip the X=Xo+UAX time. · x =- 5+0.25(20)=0 D(0,10) c(10,10) (10,7.5) 4= 40 + U AY 11. (0,40) = 3+0.25(6)=4.5 POIL ·· (x, y) = (0, 4.5) B(10,0) A (0,0) (2) When U= 0.75 X=XotHAX × = -5+0.75(2w)=10 YE YO + ULY = 3+0.75(8)=7.5 : (X,Y) = (10,7.5).

Liang-Barsky Algorithm



Х

- Numerical
- Find visible portion of the line between points
- P1(x0,y0) = (6,12)
- P2(x1,y1) = (24,18)

(10,20) (20,20) (10,10) (20,10)

- P1(x0,y0) = (12,30)
- P2(x1,y1) = (16,4)







- For polygon clipping, we require an algorithm that will generate one or more closed areas that are then scan converted for the appropriate area fill.
- What we really want to display is a bounded area after clipping.







Sutherland Hodgeman Polygon Clipping

- Beginning with the initial set of polygon vertices, we could first clip the polygon against the left rectangle boundary to produce a new sequence of vertices.
- The new set of vertices could then k successively passed to a right boundary clipper, a bottom boundary clipper, and a top boundary clipper.



Four Cases Out-In, In-In, In-out, Out-out



Figure 6-20

Successive processing of pairs of polygon vertices against the left window boundary.



Sutherland Hodgeman Polygon Clipping

As each pair of adjacent polygon vertices is passed to a window boundary clipper, we make the following tests:

(1) Out-In - If the first vertex is outside the window boundary and the second vertex is inside, both the intersection point of the polygon edge with the window boundary and the second vertex are added to the output vertex list.

(2) *In-In* If both input vertices are inside the window boundary, **only the second vertex** is added to the output vertex list.

(3) **In-Out-** If the first vertex is inside the window boundary and second vertex is outside the boundary, **only the edge intersection with the window boundary is added** to the output vertex list.

(4) **Out-Out-** If both input vertices are outside the window boundary, **nothing** is added to the output list.

Example







Q.) CLIP POLYGON ABODE AGAINST WINDOW PORS. THE CO-ORDINATES OF THE POLYGON ARE A(80,200); B(220,120); C (150,100); D(100,30); E(10,120). CO-ORDINATES OF THE WINDOW ME P(200,50); B(50,10); R(200,150); B(50,50) STEP I : PLOT THE POINTS (Xnin ; Ymax) (Xmax, Ymax) (Xmin 1 ymin) amer, ymin








GON ABODE AGAINST WINDOW PORS. THE CO- OSTEP 4: BOTTOM THE POLYGON ARE A(80,200); 8(220,120); CUPPING 100, 30); E(10, 120). CO-ORDINATES OF THE WINDOW + VERTEX CASE O/P (50,10) R (200,150), S(50,50) in-7in AA PLOT THE POINTS A (80, 200) AB in ->In 8 ymax) B'C (ac, 91)0 intin (Xmax, Ymax) in -Tout CD. (200,100) DD outin D" NE 8 (220,120) in tin E E in ->in (10,120) £(100,100) OSTEP 5 : TOP CUPPING VERTEX CASE OIP AA OUT-JID A"A Sco. DOV AID 10-710 BUUD (200,50) 810 in-pin cc' yrin in->m D(100, 30) *mex, ymin) In -> in D"D' m - in DI New DEA vertices in - rin E' in -Pout EI





Weiler And Atherton Polygon Clipping



References

- <u>https://www.youtube.com/watch?v=RGSnIK4-BhI</u>
- <u>https://www.cs.helsinki.fi/group/goa/viewing/leikkaus/lineClip.html</u> For Liang Barsky Algorithm
- <u>https://www.youtube.com/watch?v=N5Sxq3kuc_0</u> Weiler And Atherton Polygon Clipping
- https://www.youtube.com/watch?v=LCMyWFxeuro&list=PLsyTslBOa4 NwekHdOyE1Dg8eV4lJsyyd7